Long-Time Coherent Integration for Non-Radial Moving Target Based on Radon Fourier Transform with Modified Variant Angle

Denghui YAO†, Xiaoyong ZHANG‡, Zhengbo SUN††, Nonmembers, and Dexiu HU†, Member

SUMMARY  Long-term coherent integration can significantly improve the ability to detect maneuvering targets by radar. Especially for weak targets, longer integration times are needed to improve. But for non-radially moving targets, the time-varying angle between target moving direction and radar line of sight will cause non-linear range migration (NLRM) and non-linear Doppler frequency migration (NLDFM) within long-time coherent processing, which precludes existing methods that ignore angle changes, and seriously degrades the performance of coherent integration. To solve this problem, an efficient method based on Radon Fourier transform (RFT) with modified variant angle model (ARFT) is proposed. In this method, a new parameter angle is introduced to optimize the target motion model, and the NLRM and NLDFM are eliminated by range-velocity-angle joint three-dimensional searching of ARFT. Compared with conventional algorithms, the proposed method can more accurately compensate for the NLRM and NLDFM, thus achieving better integration performance and detection probability for non-radial moving weak targets. Numerical simulations verify the effectiveness and advantages of the proposed method.

key words: long-time coherent integration, moving target detection, Radon Fourier transform, variant angle model

1. Introduction

Radar is an important tool for detecting targets regardless of time or weather. But with the rapid development of stealth technology, maneuvering targets are becoming difficult to detect, making radar detection very problematic [1]–[6]. Fortunately, long-term coherent integration is an effective method to enhance the capability of moving target detection since it can provide the highest signal-to-noise ratio (SNR) gain [7]–[10]. However, with the increasing of integration time, the complex motions of maneuvering targets, e.g., high velocity and acceleration, will generate range migration (RM) [11]–[13] and Doppler frequency migration (DFM) [14], [15] both of which seriously degrade the performance. Therefore, effectively compensating RM and DFM has become a hot topic in the field of radar signal processing.

Moving target detection (MTD) is a simple coherent integration algorithm without the elimination of RM and DFM, but the poor performance limits the application. To correct RM, axis rotation-moving target detection (AR-MTD) [16] is proposed, which is implemented by range-velocity two-dimensional (2D) searching process. Methods adopting keystone transform (KT) [17], [18] can solve the linear RM without any prior knowledge via scaling the echo signal in the slow time domain. On this basis, the second-order KT (SKT) [19], [20] is proposed to eliminate the quadratic RM, namely, range curvature. Moreover, to resolve Doppler ambiguity, KT needs to combine transforms, i.e., Chirp-Z [21], Dechirping [22]. Radon Fourier transform (RFT) [23]–[25] utilizes Radon transform to extract the echo signal from the range-velocity plane and construct a Doppler matched filter to compensate for the RM, effectively integrating the constant velocity targets even in the case of Doppler ambiguity. In addition, generalized RFT (GRFT) [26] is the expansion of RFT for dealing with complex motion targets.

On the other hand, the algorithms on the DFM compensation, which is induced by target high-order motion, have also been sufficient in recent years. Due to the echo signal of maneuvering targets with constant acceleration can be modeled as a linear frequency modulated (LFM) signal, a wide variety of time-frequency analysis tools are employed to analyze the signal and eliminate DFM, e.g., Fractional Fourier transform (FRFT) [27], Lv’s distribution (LVD) [28]. FRFT is an upgraded version of Fourier transform with the function of converting LFM signals to impulse signals, thus it has a good energy concentration property for accelerated targets. KT-FRFT [29], Radon-FrFT (RFRFT) [30], and improved AR-FRFT (IAR-FRFT) [31] are applicable for the removal of DFM. LVD is a new method for signal analysis that has been reported to provide the improved detection ability of LFM signals. KT-LVD [32] and Radon-LVD (RLVD) [33] are proposed to deal with RM and DFM.

The aforementioned methods have good performance in their respective scenes, but most of them need to suppose that the angle between the target motion direction and the radar line of sight (RLOS) remains unchanged within long-term integration when establishing the target motion model. This hypothesis obviously holds for radial moving targets. Unfortunately, the trajectory of targets strictly satisfying the radial is rare, and most targets detected by radar are moving in a non-radial direction in practice. For non-radial moving targets, the angle between its trajectory and RLOS is time-varying. More seriously, the changing angle causes the target trajectory becomes more complicated and creates non-linear RM (NLRM) and non-linear DFM (NLDFM). If the conventional methods based on the assumption of invariant angle are stubbornly utilized to deal...
with non-radial moving targets, it will mismatch the model between target and algorithm, inevitably failing to eliminate NLRM and NLDFM and degrading the performance of integration. In order to keep the algorithm working properly, the current methods have no choice but to perform under a limited time in which the angle approximately maintains constant. But this way of sacrificing integration time leads to an irreconcilable contradiction between integration time and integration gain. On the one hand, the time must be increased to improve gain for detecting the weak targets. On the other hand, the increase in time will produce more serious NLRM and NLDFM, which cause gain to decrease.

To solve the above problems, this paper proposes a method based on RFT with a modified variant angle (ARFT) to compensate for the NLRM and NLDFM. As we know, RFT-based algorithms have been studied extensively, and some modified RFT methods have been recently proposed in the existing literature. Unfortunately, they did not consider the impact of angle change on long-term coherent integration and the incorrect motion model was used for dealing with NLRM and NLDFM. Thus, the proposal and application of the ARFT are significant for the long-time coherent integration of non-radial moving targets, which is very common in practice. In this method, the angle between the target motion direction and RLOS is set as a new parameter to modify the target motion model. Then the two-dimensional (2D) search with range-velocity of RFT is expanded to three-dimensional (3D) search with the range-velocity-angle. Simulation results validate the effectiveness of the proposed method for non-radial moving target integration and detection.

This paper is organized as follows. Section 2 establishes the signal model. Section 3 introduces the principle of the proposed method. Then, Sect. 4 gives a series of numerical simulations. Finally, Sect. 5 concludes this paper.

2. Signal Model and Problem Formulation

Suppose that the radar transmits a LFM signal, which can be written as:

\[
s_r(t_k, t_m) = A_0 \text{rect} \left( \frac{t_k - \frac{2R(t_m)}{c}}{t_p} \right) \exp \left\{ j\pi K \left[ t_k - \frac{2R(t_m)}{c} \right]^2 \right\} \times \exp \left\{ -j2\pi f_c \frac{2R(t_m)}{c} \right\}.
\]

(3)

where \( A_0 \) is the target reflectivity, \( c \) is the speed of light, \( R(t_m) \) is the instantaneous slant range between the radar and target. Use match filter \( h(t_k) = \text{rect} \left( \frac{t_k}{t_p} \right) \exp \left\{ j\pi K t_k^2 \right\} \) and according to stationary phase principle, the signal after pulse compression (PC) in the range-Doppler domain can be expressed as:

\[
s_{pc}(t_k, t_m) = A_1 \text{sinc} \left( B \left( t_k - \frac{2R(t_m)}{c} \right) \right) \exp \left\{ -j4\pi f_c R(t_m) \right\}.
\]

(4)

where \( A_1 \) is the amplitude after PC, \( B \) is the signal bandwidth.

It can be seen from Eq. (4) that \( R(t_m) \) will produce migration on envelope and phase of the signal. Therefore, in order to effectively compensate RM and DFM, the first step of coherent integration algorithm is accurately estimating \( R(t_m) \) and it is directly determined by the target motion model. This paper primarily discusses the effect of varying flight angles on the target motion model but does not make specific requirements for the target motion state. Therefore, the most unadorned uniform linear motion model is selected to calculate \( R(t_m) \).

Consider the scenario of target integration and detection shown in Fig. 1, a target moves with uniform speed \( v_0 \) along the non-radial direction and the initial radial slant range between target and radar is \( R_0 \), the initial angle between target motion direction and RLOS is \( \theta_0 \), and the integration time is \( t_m \). Hence, according to the conventional algorithm, the \( R(t_m) \) can be calculated as:

\[
R(t_m) = R_0 - v_0 \cos \theta_0 t_m,
\]

(5)

then we can employ Eq. (5) to compute:

\[
\text{RM} = \frac{-v_0 \cos \theta_0 t_m}{R_0}, \quad \text{DFM} = 0.
\]

(6)

From Eq. (5), we can see clearly that the angle is set to constant during coherent integration. Nevertheless, the
angle is changing, and it satisfies:

$$\theta = \arccos \frac{2R_0v_0t_m \cos \theta_0 - 2v_0^2t_m^2}{2v_0t_m \sqrt{R_0^2 + (v_0t_m)^2 - 2R_0v_0t_m \cos \theta_0}}. \quad (7)$$

It is apparent that the angle is time varying and is related to $R_0, v_0, \text{ and } \theta_0$. What is more, $R(t_m)$ varies nonlinearly with $t_m$ and produces NLRM and NLDFM, which are inconsistent with the calculation of Eq. (5) and Eq. (6). Thus, when dealing with non-radial moving targets, the current methods have errors in calculating $R(t_m)$ due to the wrong assumption, and the uncompensated NLRM and NLDFM will bring significant problems to coherent integration.

3. **Coherent Integration Based on ARFT**

In this section, a method called ARFT is proposed to realize the coherent integration for non-radial moving targets.

3.1 **Variant Angle Model**

As the analysis in Sect. 2, we know that the non-radial moving targets generate NLRM and NLDFM and inevitably impact the performance of conventional methods. To address this problem, we introduce a modified motion model with a variant angle and the geometric diagram as shown in Fig. 2.

In this model, the angle namely $\theta(t_m)$ is set as a new parameter which is varying with $t_m$ during integration. Thus, we can use the cosine theorem to rewrite the equations of $R(t_m)$ as:

$$R(t_m) = \sqrt{R_0^2 + (v_0t_m)^2 - 2R_0v_0t_m \cos \theta_0}, \quad (8)$$

then RM and DFM are derived as follows:

$$\text{RM} = \sqrt{R_0^2 + (v_0t_m)^2 - 2R_0v_0t_m \cos \theta_0} - R_0,$$

$$\text{DFM} = \frac{2v_0 [\cos \theta(t_m) - \cos \theta_0]}{\lambda}, \quad (9)$$

$\lambda$ is signal wavelength. Compared with the traditional model, Eq. (8) and Eq. (9) match the real motion of the target. Hence, $R(t_m)$ can be estimated more accurately thanks to the introduction of $\theta(t_m)$ and it makes preparation for correction of NLRM and NLDFM.

![Fig. 2 Modified variant angle model for non-radial moving targets.](image)

3.2 **Correction and Integration**

After optimizing the target motion model using variant angle, we apply Eq. (8) into Eq. (4) produce:

$$s_{pc}(t_k, t_m) = A_1 \text{sinc} \left[ B \left( t_k - \frac{2 \sqrt{R_0^2 + (v_0t_m)^2 - 2R_0v_0t_m \cos \theta_0}}{c} \right) \right] \exp \left[ \frac{-j4\pi \sqrt{R_0^2 + (v_0t_m)^2 - 2R_0v_0t_m \cos \theta_0}}{\lambda} \right]. \quad (10)$$

The NLRM and NLDFM showed in Eq. (10) must be corrected to realize coherent integration. Inspired by RFT which utilizes 2D searching of range-velocity to compensate RM and DFM, we consider the method of multidimensional unknown motion parameters searching, extracting target envelope and constructing filter array to deal with NLRM and NLDFM. Precisely for this problem, it is obvious that $R(t_m)$ relates to $R_0, v_0, \text{ and } \theta_0$. Thus, except $R_0, v_0$ which have been taken into account in original RFT, it must also add the search of $\theta_0$ on this basis to describe $R(t_m)$ in Eq. (8) more precisely. Note that the range-velocity 2D searching of RFT should be promoted to range-velocity-angle 3D searching, and we called the modified RFT with the search of angle ARFT. The process of ARFT can be formulated as follow:

$$G(r, v, \theta) =$$

$$\int_0^T \int_0^{t_r} s_{pc}(t_k, t_m) \delta \left[ t_k - \frac{2 \sqrt{r^2 + (vt_m)^2 - 2rt_m \cos \theta}}{c} \right] \text{H}_{\text{rfa}}(t_m) dt_k dt_m,$$

where $G$ denotes the coherent integration result of ARFT, $T$ is total integration time, $r, v, \text{ and } \theta$ are the search value of the initial range, velocity and angle respectively, $\delta(t)$ is the impulse function and $\text{H}_{\text{rfa}}(t_m)$ represents Doppler filter function which is defined as:

$$\text{H}_{\text{rfa}}(t_m) = \exp \left[ \frac{-j4\pi \sqrt{R_0^2 + (v_0t_m)^2 - 2R_0v_0t_m \cos \theta_0}}{\lambda} \right]. \quad (12)$$

As shown in Eq. (11), $\delta(t_k)$ serves to extract the target from the fast time-slow time domain and concentrate signal energy into one range cell, which can estimate NLRM. On the other hand, $\text{H}_{\text{rfa}}(t_m)$ plays a role in compensating the phase fluctuation, which can correct NLDFM. Therefore, ARFT is implemented by search within a specific scope and only when $r = R_0, v = v_0, \theta = \theta_0$, NLRM and NLDFM are completely compensated, and the maximum value of coherent integration $G_{\text{max}} = A_1 T$ is obtained.

In addition, the search scope and interval of target unknown motion parameters are crucial for the effective implementation of ARFT. Generally, the search scope is determined by the radar detection task. Assuming the
task of the radar is to detect the target within the red sector area in Fig. 3, the search scope of ARFT is \( r \in [r_{\min}, r_{\max}], v \in [v_{\min}, v_{\max}], \theta \in [\theta_{\min}, \theta_{\max}] \).

While the search interval is related to the signal and system parameters, specifically, the range search interval \( \Delta r = \frac{r_{\max} - r_{\min}}{N_r} \), the velocity search interval \( \Delta v = \frac{v_{\max} - v_{\min}}{N_v} \), the angle search interval sets as 3 dB beam width of antenna, \( \Delta \theta = 0.89 \frac{D}{T} \), where \( D \) is the antenna aperture. Then, the range, velocity, and angle search amount \( N_r, N_v, N_\theta \) can be calculated as follows:

\[
N_r = \text{round} \left( \frac{r_{\max} - r_{\min}}{\Delta r} \right), \quad N_v = \text{round} \left( \frac{v_{\max} - v_{\min}}{\Delta v} \right),
\]

\[
N_\theta = \text{round} \left( \frac{\theta_{\max} - \theta_{\min}}{\Delta \theta} \right),
\]

(13)

where \( \text{round}() \) denotes the integer operator.

Thus, ARFT can be further expressed as:

\[
G_{\text{ARFT}} = \max_{x, t_0} \int_{0}^{T} |H_{x,t_0}(t_m)| dt_m,
\]

(14)

where \( r = r_{\min} + n_r \Delta r, \quad v = v_{\min} + n_v \Delta v, \quad \theta = \theta_{\min} + n_\theta \Delta \theta \).

The flowchart of the proposed method can be summarized as shown in Fig. 4:

According to the analysis, ARFT is one of the optimized coherent integration methods of RFT. Like RFT-based methods, ARFT also extracts echo signals from the fast time-slow time domain via parameters searching, but the target motion model is different. Hence, it is necessary to make a comparison between ARFT and RFT-based methods.

We can reconsider Eq. (8) and take Taylor series expansion of it:

\[
R(t_m) = R_0 - v_0 \cos \theta_0 t_m + \frac{v_0^2}{2 R_0} (1 - \cos^2 \theta_0) t_m^2 + \sum_{n=3} R^{(n)}(0) \left( \frac{t_m}{n!} \right)^n,
\]

(15)

on the contrary, RFT calculate the \( R(t_m) \) as Eq. (5). And second-order algorithm i.e., GRFT calculate the \( R(t_m) \) as:

\[
R(t_m) = R_0 - v_0 \cos \theta_0 t_m + \frac{1}{2} a_0 \cos \theta_0 t_m^2,
\]

(16)

where \( a_0 = v_0^2/R_0 \) is target acceleration. Different models make different results of signal extraction. For comparative analysis, we set a non-radial moving target with, \( R_0 = 100 \) km, \( v_0 = 1000 \) m/s, \( \theta_0 = 120^\circ \), and the extraction results of RFT, GRFT, ARFT and the real target trajectory are shown in Fig. 5:

We can see that RFT and GRFT respectively use a line and parabola to extract signals inconsistent with the target real motion state, while ARFT applies a curve with the angle to extract signal correctly. Similarly, the phase compensation functions of RFT and GRFT also have errors, while ARFT can accurately match the target phase. This theoretically explains why the proposed algorithm is more universal for non-radial moving targets than other RFT-based algorithms.

### 3.3 Coherent Integration Time Comparison

We can obviously find that Eq. (5) and Eq. (16) are first-order and second-order expressions of Eq. (15) after ignoring the higher-order term. This simplification must have
approximation errors, which inevitably provoke the loss in coherent integration, we call it model loss, namely $L$. Assuming that the initial SNR is $S_0$ and the gain of coherent integration is $g$. Thus, the output SNR is $S_0 + g - L$. To successfully detect the target, $S_0 + g - L \geq D_0$ must be met, where $D_0$ is minimum detectable SNR. In other words, there must be:

$$L \leq S_0 + g - D_0.$$  \hfill (17)

Unfortunately, $L$ increases with integration time, and when it cannot satisfy the Eq. (17), target detection will fail. Therefore, the integration time constraint relationship can be summarized as Fig. 6:

Note that $D_0$ determines the maximum allowed value of $L$, and $L$ limits the maximum integration time. What is more, we discuss the scene in Fig. 7:

As shown in Fig. 7, a target is moving at a uniform speed $v$, $R(t_0)$ and $R(t_m)$ respectively denote the initial and instantaneous slant range between the radar and target, $\Delta R = R(t_m) - (R_0 + v_0 t_0 \cos \theta_0)$ is the approximate errors of conventional methods, i.e., RFT and GRFT. $\Delta R_{\text{max}}$ is the maximum tolerable, which must obey $\Delta R \leq \Delta R_{\text{max}}$ at any time. Thus, when $\Delta R_{\text{max}}$ is determined, then the maximum integration time, namely $t_L$ is determined. Accordingly, as shown in Fig. 7, the maximum coherent integration time of conventional methods is limited to $t_L$. On the contrary, the proposed algorithm can coherently integrate $t_P$. Although like $t_L$, both of them are limited by the target motion state, and the integration time will be shortened when the target no longer maintains a uniform linear motion. But $t_P$ is not limited by the variation of flight angle, thus it is significantly longer than $t_L$.

### 3.4 Computational Complexity Analysis

Assume that $N_r$, $N_v$, $N_a$, $N_\theta$, $M$ respectively represent the number of searching range, searching velocity, searching acceleration cells, searching angle, and integration pulses number. The computational complexities of RFT, GRFT, and the proposed method are analyzed in Table 1.

Table 1 illustrates that the proposed ARFT has comparable computational complexity to GRFT since they are both 3-D parameters search. Compared with ARFT and GRFT, the computational complexity of RFT is lower since it only performs 2-D searching. Thus, the proposed method has no superiority in terms of computation.

### 4. Numerical Experiments

In this section, several numerical simulations are conducted to analyze the coherent integration performance and detection probability of the proposed method for a maneuvering target with uniform velocity in a non-radial direction under the Gaussian noise environment. The results of MTD, RFT, and GFRT are also given for comparison.

#### 4.1 Coherent Integration for Weak Target

To begin with, we evaluate the coherent integration for a weak target, where the simulation parameters are given in Table 2.

Figure 8(a) shows the signal after pulse compression, illustrating that the target is completely buried in the noise. To clearly show the target’s trajectory, the signal after pulse compression without noise is given in Fig. 8(b), and it can be seen that serious NLRM is due to the high speed and variant angle. Without eliminating NLRM and NLDFM, MTD fails to detect the target, which is shown in Fig. 8(c). Moreover, the coherent integration results of RFT and GRFT,
Fig. 8 Coherent integration for a weak target via MTD, RFT, GRFT, and ARFT. (a) Result after pulse compression. (b) Result after pulse compression without noise. (c) MTD (d) RFT (e) GRFT (f) ARFT in range-velocity domain (g) ARFT in angle domain.

respectively shown in Fig. 8(d) and Fig. 8(e), are ineffective due to integration loss caused by the mismatch between model and target. Instead, Fig. 8(f) and Fig. 8(g) show the result of the proposed method in range-velocity dimensions (θ₀ = 95.71°) and angle dimension (r₀ = 100.5 km, v₀ = 1000 m/s), respectively. We can obviously find that the target energy is coherently integrated as one remarkable peak, which implies better coherent integration ability for weak targets.

4.2 Coherent Integration for Multiple Targets

When detecting multiple targets, ARFT adopts an iterative solution based on Eq. (14), and the specific operations are as follows:

(1) The first target result is obtained by searching the maximum value according to the ARFT algorithm, and the detection is completed combined with Constant False-Alarm Rate (CFAR) detector for detection. (2) The first target is removed from the search grid, and then ARFT is used to search the next target. CFAR is also used for detection. (3) Repeat the above process until there is no target in the CFAR detector result, and it is considered that multiple targets detection has been completed.

To prove the validity of the proposed method for multiple targets’ coherent integration, two non-radial moving targets are analyzed in the experiment, and the motion parameters of the targets are listed in Table 3. To prove the validity of the proposed method for multiple targets’ coherent integration, two non-radial moving targets are analyzed
in the experiment and the motion parameters of the targets are listed in Table 3.

Figure 9(a) shows the result after pulse compression. Besides, Fig. 9(b) and Fig. 9(c) respectively show the range-velocity search results of target A and target B via ARFT. We can clearly see targets emerge from the noise and form two sharp peaks, which are helpful for target detection. As shown in Fig. 9(d) and Fig. 9(e), two obvious peaks appear in the corresponding angle domain and demonstrate the availability of the proposed method for multiple targets. What is more, the peak values indicate the estimated motion parameters of target A and target B equal to simulation settings.

4.3 Targets Detection Ability

Furthermore, the target detection ability of MTD, RFT, GRFT, and proposed ARFT have been investigated by Monte Carlo trials. Complex white Gaussian noise with zero mean is added to the signal after pulse compression to yield SNRs varying from $-25$ dB to 15 dB. And for each SNR value, 1000 simulations are performed. We combine the CFAR detectors and the four methods as corresponding detectors. Besides, the false alarm ratio is set as $P_{fa} = 10^{-2}$. Other parameters are the same as Table 2 and the integration time is 1 s. The curves of detection probability ($P_d$) are shown in Fig. 10.

According to the results, for $P_d > 90\%$, the needed minimum SNR of MTD, RFT, GRFT, and ARFT is respectively 10 dB, 6 dB, $-15$ dB, $-20$ dB. Thus, other methods suffer from obvious detection performance loss compared to the proposed method. Moreover, when SNR = $-19$ dB, the of MTD, RFT, GRFT, and ARFT are respectively 1%, 1%, 14%, and 97%. Hence, it is apparent that the proposed ARFT is superior to MTD, RFT, and GRFT when dealing with non-radial moving targets due to its variant angle model to solve the NLRM and NLDFM.

4.4 Performance Analysis in Different Scenarios

As discussed above, the NLRM and NLDFM are related to the integration time, target velocity, and initial angle. Thus, in the following subsection, we separately change time, velocity, angle and analyze the detection probability of the RFT, GRFT, and ARFT to compare the stability and robustness under different conditions. Monte Carlo experiments are conducted and for each value, 1000 independent simulations are performed. Parameters of radar are given in Table 2 and the SNR after pulse compression is $-20$ dB.

First, curves in Fig. 11 show the result of the three
methods under different integration times, which vary from 0.5 to 5 s. Note that the initial range, initial velocity, and initial angle of the non-radial moving target are 100.5 km, 1000 m/s, and 95.71°. It can be seen that the performance of RFT and GRFT is close to ARFT since the beginning. Nevertheless, when the time rises to a certain degree, they do not increase but fall rapidly. This is because their models have integration loss which is more severe with the increase of time, reflecting the time limitation of the conventional methods for long-time integration of non-radial moving targets. In contrast, the $P_d$ of ARFT steadily improves with integration time thanks to the modification of the model.

Next, we evaluate the detection ability varies with initial target velocities, and the result is shown in Fig. 12. In addition, the initial range and initial angle of the non-radial moving target are 100.5 km, 95.71° and the integration time is 1 s. From Fig. 12, we can see that when $v_0 = 0$, the four methods have identical performance because a stationary target does not cause NLRM and NLDFM. While, the increase of velocity, MTD, RFT, and GRFT decrease successively due to the unprocessed NLRM and NLDFM. On the other hand, the $P_d$ of ARFT is consistently above 95%, maintaining good performance.

Finally, Fig. 13 shows that the fluctuation of $P_d$ varies with angles. Besides, the initial range and initial angle of the non-radial moving target are 100.5 km, 95.71° and the integration time is 1 s. It is obvious that $P_d$ of MTD is almost zero, while RFT, GRFT are close to ARFT at first, whereas they suddenly drop with the increase of angle. On the contrary, $P_d$ of ARFT stables at a high level. This is because when the angle is slight, the target motion model can be regarded as a radial model. Furthermore, the NLRM and NLDFM are approximately RM and DFM, thus RFT and GRFT can be effectively performed. Unfortunately, as the angle increases, these methods are gradually invalid.

Consequently, through the above three groups of experiments, it is proved that the ARFT has good stability and practicability for detecting non-radial moving targets.

5. Conclusions

To address the NLRM and NLDFM induced by non-radial moving targets, this paper proposed a method called ARFT. Specifically, ARFT modified the target motion model via changing the angle between target motion direction and RLOS from original constant to variable and adopted motion parameters searching of range-velocity-angle based on RFT to compensate for the NLRM and NLDFM. Compared with conventional methods, i.e., MTD, RFT, and GRFT, the proposed method can: (a) achieve more satisfactory integration performance for weak targets because the limitation of integration time has been eliminated by the introduction of
variant angle; (b) obtain better target detection ability for non-radial moving targets due to the precise and meticulous motion model. Meanwhile, the simulation results demonstrated the availability of the proposed method. Moreover, we will focus on the long-time coherent integration of maneuvering non-radial moving targets with acceleration or curve trajectory in the subsequent work.

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References

Denghui Yao received the B.S. degree from the University of Electronic Science and Technology of China, in 2019 and he is currently pursuing the M.S. degree in Information Engineering University. His research interests include radar detection and signal processing.

Xiaoyong Zhang received the Ph.D. degree from the National Key Laboratory of Science and Technology on Blind Signal Processing, in 2011. His research interests include radar detection and signal processing.

Zhengbo Sun received the B.S. degree from the University of Electronic Science and Technology of China, in 2019 and he is currently pursuing the M.S. degree in Information Engineering University. His research interests include radar detection and signal processing.

Dexiu Hu received the B.S. and M.S. degrees from the Zhengzhou Information Technology Institute, Zhengzhou, China, in 2007 and 2010, respectively, and the Ph.D. degree in electronic engineering from Tsinghua University, Beijing, China. He is currently an associate professor with Information Engineering University, Zhengzhou, China. His current research interests include radar signal processing and passive location.